

# A method for calculating the pK<sub>a</sub> values of small and large molecules

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## Introduction

A method was developed for predicting of the aqueous ionization constants (pK<sub>a</sub>) of organic molecules. The method is based on empirically calculated physico-chemical parameters that are obtained from ionization site-specific regression equations.

### Submit molecule



Take the major resonant form or/and the major tautomeric form



Calculating the micro pK<sub>a</sub> from empirical increments

- partial charge increment
- polarizability increment
- structure specific increments



Calculating the microspecies distribution



Assigning calculated pK<sub>a</sub> values to the atoms of the submitted molecule

*Scheme of pK<sub>a</sub> calculation*

## Calculation of pK<sub>a</sub>

pK<sub>a</sub> of the monoprotic molecules to be calculated as the sum of the next three increments.

$$pK_a = a*Q + b*P + c*S + d$$

where,

Q is the partial charge increment

P is the polarizability increment

S is sum of the structure specific increments

a, b, c, and d are regression coefficients specific to the ionization site

Structure specific increments may contain two quantities: steric strain or/and H-bond increments.

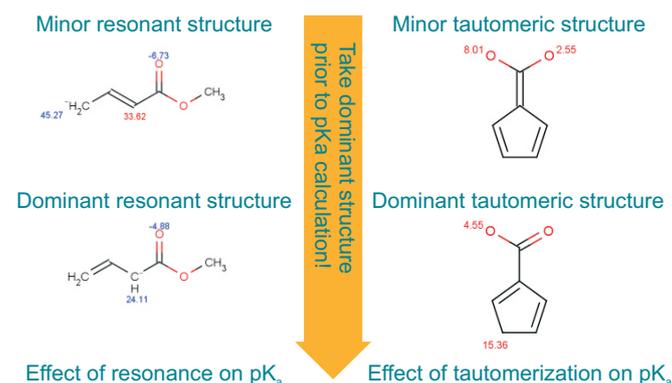
All of the pK<sub>a</sub> increments above are calculated from ionization-site specific regression equations.

We should pay special attention to molecules with a large number of ionization sites. In these molecules ionization sites may directly perturb each other through proximity effects like H-bonding or altering electron withdrawing effects by protonation/deprotonation. 'Macro effects' take place when micro pK<sub>a</sub> values of sites are close to each other, which shifts the macro pK values measured experimentally. The 'macro effect' is independent of the distance between the ionizable groups.

The pK<sub>a</sub> calculation of multiprotic molecules is governed by theoretically derived kinetic equations in our model. One of the outstanding characteristics of the theoretical expressions of the pK<sub>a</sub> calculation is that interactions among the ionizable atoms are taken into account also in the case when the ionizable atoms are far from each other. We also take advantage of this behavior in the case of large molecules that may have ionization sites far from each other. Proteins are typical molecules in this category.

One of the most difficult issues is how the effect of tautomerization and resonance can be taken into account in pK<sub>a</sub> prediction. These two isomerization processes may bring about significant difference between predicted and experimentally obtained pK<sub>a</sub>'s.

This is why we developed a preprocessing algorithm for pK<sub>a</sub> calculation which generates the most dominant tautomeric and resonant structures of the submitted molecules prior to the pK<sub>a</sub> calculation.



*Effect of resonance and tautomerization on pK<sub>a</sub> calculation*

## Types of the acidic and the basic groups in our pK<sub>a</sub> model

### Acidic groups:

1. X-AH, where X is any atom without lone pair electron which does not take part in delocalization with the surrounding atoms. e.g. ethanol
2. X-AH, where X has lone pair electron or p<sub>z</sub> orbital, e.g. acetic acid
3. AH, where A takes part in extended delocalization. e.g. pyrrole

### Type of the basic groups

Atom B should have a lone pair

### Basic groups:

1. X-B, where X is any atom without a lone pair and it does not take part in a delocalization with the surrounding atoms, e.g. methylamine
2. X-B, it has lone pair or p<sub>z</sub> orbital, e.g. amidine
3. B, where B takes part in an extended delocalization, e.g. pyridine

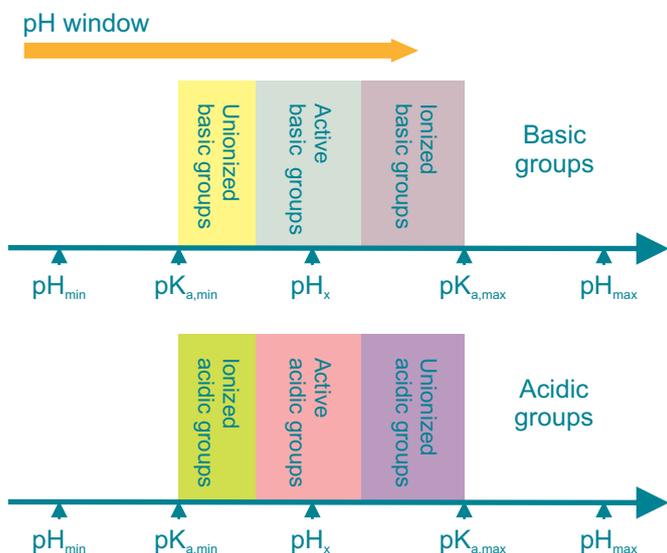
## The small and large models of pK<sub>a</sub> calculations

We use the small pK<sub>a</sub> model if the number of the ionizable atoms (N) is smaller or equals to 8.

The small pK<sub>a</sub> model generates altogether 2<sup>N</sup> microspecies from the submitted molecule.

The micro ionization constant of these microspecies are calculated with the empirical relation given above. Finally, macro pK<sub>a</sub> values are obtained from the theoretical relations that hold between macro-micro pK<sub>a</sub> values.

The large model is invoked if the number of the ionizable atoms (N) is larger than 8. Since calculation time and memory requirement strongly depends on N, therefore, we developed a so-called pH window method for reducing N. Only pivot atoms are taken into account in the pK<sub>a</sub> calculation at a given pH. This technique is described in Fig.3. below.



Only those basic or acidic groups are considered to be protonable or deprotonable at a given pH<sub>x</sub> which have a micro pK<sub>a</sub> value inside the pH window. The width of the pH window is 2 pH units. All atoms that are outside the pH window are considered inactive. Number of ionizable atoms are reduced to N=8 in this way. The reduced microspecies set contains only 2<sup>8</sup> microspecies.

pK<sub>a</sub> of the active groups at a given pH can be calculated according to this relation.

$$K_{a,i} = \frac{\prod_k c_k^{(i-1)}}{\prod_k c_k^i} H$$

where,

[H+] is the proton concentration of the aqueous solution

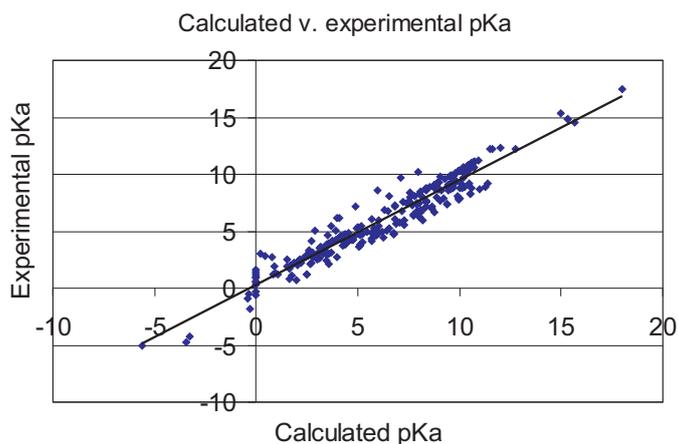
c<sub>j</sub><sup>i</sup> is the concentration of the j-th microspecies that released i protons from the fully protonated molecule

c<sub>k</sub><sup>(i-1)</sup> is the concentration of the k-th microspecies that released (i-1) protons from the fully protonated molecule

Ratio of c<sub>j</sub><sup>i</sup> and c<sub>k</sub><sup>(i-1)</sup> are calculated from the micro ionization constants

### Test of the large and the small models

For proteins we defined H-bond interaction between carboxyl (COOH) and amide groups (CONH<sub>2</sub>). Conditions of the H-bond interaction calculated from the 3D geometry of the protein.



Test results for small molecules. For a diverse set of small molecules we used the small pK<sub>a</sub> prediction model. n=269, r<sup>2</sup>=0.93, s=0.75

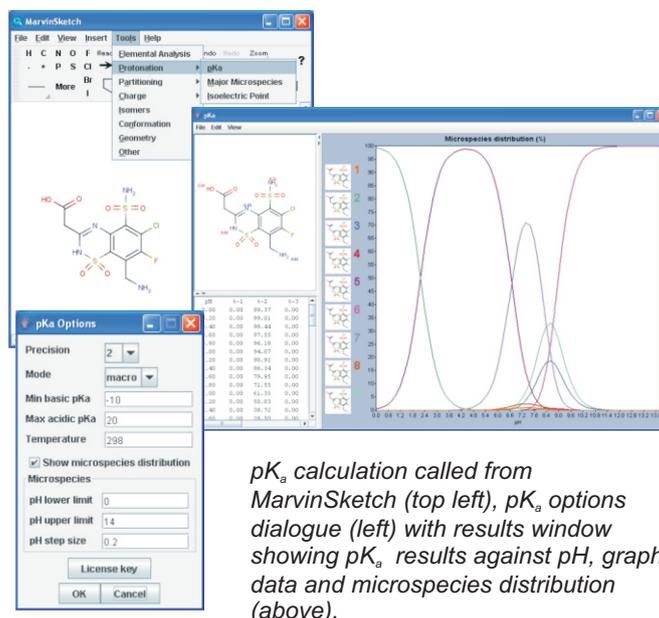
Acidic groups Predicted pK <sub>a</sub>	Residue number	Exp. pK <sub>a</sub>	Basic groups Predicted pK <sub>a</sub>	Residue number	Exp. pK <sub>a</sub>
3.55	2	-	12.20	41	
4.16	37	-	11.61	50	
4.86	7	5.60	10.19	34	
5.36	44	5.60	7.71	1	
6.14	61	7.00	-0.26	3	
9.21	73	-	-0.41	41	
9.81	10	-	-0.69	42	
14.12	23	-	-1.04	52	

Table of test results for a protein (1A91.pdb) molecule (SUBUNIT C OF THE F1FO ATP SYNTHASE OF ESCHERICHIA COLI)

### Implementation

Calculation plugins are available through Marvin and JChem software suites

Hardware and software requirements: any system running Java Runtime Environment 1.4 or above (The API is also accessible from .NET).



pK<sub>a</sub> calculation called from MarvinSketch (top left), pK<sub>a</sub> options dialogue (left) with results window showing pK<sub>a</sub> results against pH, graph data and microspecies distribution (above).